Linear and Nonlinear Viscoelastic Arterial Wall Models: Application on Animals

This work deals with the viscoelasticity of the arterial wall and its influence on the pulse waves. We describe the viscoelasticity by a nonlinear Kelvin–Voigt model in which the coefficients are fitted using experimental time series of pressure and radius measured on a sheep’s arterial network. We obtained a good agreement between the results of the nonlinear Kelvin–Voigt model and the experimental measurements. We found that the viscoelastic relaxation time—defined by the ratio between the viscoelastic coefficient and the Young’s modulus—is nearly constant throughout the network. Therefore, as it is well known that smaller arteries are stiffer, the viscoelastic coefficient rises when approaching the peripheral sites to compensate the rise of the Young’s modulus, resulting in a higher damping effect. We incorporated the fitted viscoelastic coefficients in a nonlinear 1D fluid model to compute the pulse waves in the network. The damping effect of viscoelasticity on the high-frequency waves is clear especially at the peripheral sites.

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1 Introduction

One way of obtaining information about the cardiovascular system is by studying pressure and flow waveforms. By analyzing and modeling flow waveforms, we can deduce the mechanical properties of the cardiovascular system even in regions of the network inaccessible to visualization techniques. However, challenges still remain such as real-time observations and analysis of flow waveforms to help the medical staff make diagnostics and surgical decisions. Pulse waves of pressure and flow rate in the arterial system can be correctly captured by 1D models of blood flow. The 1D approach is attractive because it is a good compromise between modeling complexity and computational cost and is useful for medical applications, such as disease diagnostic and presurgical planning. Difficulties arise when performing patient-specific simulations as the number of parameters required by the model increases with the number of simulated arterial segments. The hardest parameters to obtain are those describing the complex mechanical properties of the arterial wall. In the 1D model, a constitutive equation of the wall mechanics is necessary to close the system of conservation laws of mass and momentum. Although the viscoelastic behavior of the wall has been recognized as fundamental for a long time, most 1D numerical simulations existing in literature adopted elastic wall models for simplicity since the viscoelastic coefficient is difficult to measure. Another problematic point is that the viscoelastic response of the wall dynamics interacts with the viscoelastic properties of the blood. Therefore, both phenomena should be included in the model to obtain a complete picture of the coupled wall-blood flow dynamics even though it was shown that differentiating both behaviors from experimental data is a complicated task [1].

Nevertheless, there are previous studies of blood flow in networks using viscoelastic 1D models. The viscoelastic models for the arterial wall fall into roughly two categories: Fung’s quasi-linear viscoelastic models [2] and an arrangement of spring–dashpot elements. Models of the first category are more general but also more difficult to handle when coupled with a 1D model of blood flow because they involve a creep function and convolutions have to be computed [3]. Holenstein et al. [4] proposed a model and fitted the parameters from published data. Raymond et al. [5,6] adopted Holenstein’s model and parameter values in their patient-specific simulations. Comparison between numerical results and in vivo measurements reveals a considerable impact of the viscoelasticity on the pulse waves. Another comparison between the results obtained with 1D models using different viscoelastic models of the first category shows that the differences between the results computed with different models are minor [7]. Segers et al. [8] proposed another approach incorporating a frequency-dependent viscoelastic model with the linearized 1D model of blood flow. They found that the influence of viscoelasticity is comparable to the elastic nonlinearity [7]. We note that the parameter values of the viscoelastic model are fitted from the limited available data in literature.

The second class of viscoelastic models is built by combinations of springs and dashpots. The Kelvin–Voigt model which consists of one spring and one dashpot connected in parallel is suitable to describe viscoelastic solids and is straightforward to incorporate in a 1D model of blood flow. Armentano et al. [9] fitted the coefficients of the Kelvin–Voigt model from simultaneous experimental measurements of diameter and pressure and obtained acceptable agreements with measurements.
Alastruey et al. [10] also adopted the Kelvin–Voigt model and estimated the parameters using a tensile test. They simulated the pulsatile flow in an in vitro experimental setup and compared this model with an elastic one. They showed that the viscoelastic model agrees much better with measurements than the elastic one. We observe furthermore that the vessels in the study were made of polymers which are actually much less viscous than the real arterial wall.

In this paper, we propose to analyze a nonlinear Kelvin–Voigt wall model and to study the effect of viscoelasticity on the pulse waves of a sheep’s arterial networks. We collected simultaneous time series of diameter and pressure at different arterial sites from a group of sheep (experimental data from Ref. [11]). We estimated the viscoelasticity coefficients by fitting the experimental measurements using the following nonlinear Kelvin–Voigt model:

\[
(1 - \eta^2) \frac{R}{h} P = E \dot{e} + \phi_0 \ddot{e} + \phi_{NL} \dddot{e}^2
\]

where the nonlinear coefficient \( \phi_{NL} \) appears necessary to retrieve the experimental data. Segers et al. [8] have shown that the nonlinear term in \( \dddot{e}^2 \) can be neglected compared to \( \ddot{e} \). We have confirmed this fact, and therefore, we have removed the corresponding term in the proposed viscoelastic model. Conversely, the nonlinear term in \( \dddot{e}^2 \) seems to play an important role in the wall dynamics. Erbay et al. [12] used this nonlinear term to study the wave propagation in nonlinear viscoelastic tubes, and the theoretical basis of the approach is in Ref. [13].

We computed the unsteady blood flow in the network using a 1D blood flow model coupled to the linear viscoelastic wall model. We observed the smoothing effect of the wall viscosity on the pulse waveforms in particular at the terminal sites of the network. This result is corroborated by the observation that the viscoelastic relaxation time \( \phi_0/E \) is nearly constant throughout the network. Therefore, as it is well known that smaller arteries are stiffer, the viscoelastic coefficient rises when approaching the peripheral sites to compensate the increase of the Young’s modulus, resulting in a higher damping effect.

Section 2 presents the experimental protocol for data acquisition, the proposed nonlinear Kelvin–Voigt model, the optimization approach to compute the model parameters, and the 1D blood flow model used in the numerical simulations. In Sec. 3, we discuss the optimization results and the numerical findings. We also present numerical simulations to explain the differences between an elastic and a viscoelastic wall model.

2 Methodology

2.1 Data Acquisition. The experimental data were obtained from a group of 11 sheep (male Merino, between 25 and 35 kg). Before surgeries, the animals were anesthetized with sodium pentobarbital (35 mg/kg). The arterial segments of interest (6 cm long) were separated from the surrounding tissues. To measure the diameter, two miniature piezoelectric crystal transducers (5 MHz, 2 mm in diameter) were sutured on opposite sides into the arterial adventitia. The animals were then sacrificed, and the arterial segments of interest were excised for in vitro tests.

The arterial segments were mounted on a test bench where a periodical flow was generated by an artificial heart (Jarvik Model 5, Kolff Medical, Inc., Salt Lake City, UT). The input signal was close as possible to a physiological waveform. We obtained the desired pressure waveforms by simple adjustments of tuning resistances and Windkessel chambers.

The circulating liquid was an aqueous solution of Tyrode. At each arterial segment, the internal pressure was measured using a solid-state pressure microtransducer (Model P2.5, Konigsberg Instruments, Inc., Pasadena, CA), previously calibrated using a mercury manometer at 37 °C. The arterial diameter signal was calibrated in millimeters using the 1 mm step calibration option of the sonomicrometer (Model 120, Triton Technology, San Diego, CA). The transit time of the ultrasonic signal with a velocity of 1580 m/s was converted to the vessel diameter.

The experimental protocol was conformed to the European Convention for the Protection of Vertebrate Animals Used for Experimental and Other Scientific Purposes. For more details on the animal experiments, refer to Ref. [11].

The synchronized recording of transmural pressure and diastolic pressure was applied on the following seven anatomical locations as shown in Fig. 1: ascending aorta (AA), proximal descending aorta (PD), medial descending aorta (MD), distal descending aorta (DD), brachiocephalic trunk (BT), carotid artery (CA), and femoral artery (FA).

We note that the experimental data were acquired from blood vessels that are extracted from their surrounding tissue and this modifies the experimental “pressure–radius” function we will use to do the optimization process. Others factors modifying this relation are listed in Ref. [14], where it was shown that arterial wall viscosity and elasticity were influenced by adventitia removal in in vivo studies, possibly by a smooth muscle-dependent mechanism.

2.2 Nonlinear Wall Model and Evaluation of the Parameters. In a linear approach for an isotropic, incompressible, and homogeneous arterial wall with a thickness \( h \) and radius \( R \), the thin cylinder theory states that the stress \( \sigma \) and the linearized strain \( \varepsilon = R - R_0/R_0 \) follow the equation:

\[
\sigma = \frac{E}{(1 - \eta^2)} \varepsilon
\]

where \( E \) is the Young’s modulus, \( R_0 \) is the unstressed radius, and \( \eta \) is the Poisson ratio (0.5 for incompressible materials). Also, the transmural pressure \( P - P_{ext} \) is related to the stress \( \sigma \) by the equation

\[
\sigma = \frac{R(P - P_{ext})}{h}
\]

The reader can refer to Ref. [15] for details. Conform to the experimental setup, we set the external pressure to zero and we have

\[
(1 - \eta^2) \frac{R}{h} P = E \dot{e}
\]

the equation linking the pressure \( P \) to the strain \( e \). Adding to the right-hand side a viscoelastic term \( \phi \dot{e} \), where \( \phi \) is the coefficient modeling the wall viscosity, we retrieve a classic Kelvin–Voigt model. We can build a more general nonlinear wall model by developing \( e \) and \( \dot{e} \) asymptotically to second-order, we then find

\[
(1 - \eta^2) \frac{R}{h} P = E \dot{e} + E_{NL} \ddot{e}^2 + \phi_0 \ddot{e} + \phi_{NL} \dddot{e}^2
\]

where the subscript \( NL \) stands for nonlinear and we have \( E_{NL} \ll E \).

Fig. 1 Arterial tree of a sheep. Experimental data are collected from 11 sheep at the following seven locations: ascending aorta (AA), proximal descending aorta (PD), medial descending aorta (MD), distal descending aorta (DD), brachiocephalic trunk (BT), carotid artery (CA), and femoral artery (FA). There are three virtual arteries (VAs), which are indicated by dashed lines, to model the side branches when pulse waves are simulated. Parameters for all the arteries are shown in Table 1.
The thickness through a loop in the calculation. The pseudocode is:

Step 1: Evaluate the DFT of R (assume N as an even number without loss of generality)

\[ \tilde{R}_k = \frac{1}{N} \sum_{n=0}^{N-1} R_n \cdot e^{-\frac{2\pi i nk}{N}} \]

Step 2: \(|\tilde{R}_k|\) represents the amplitude of the kth wave. To filter out the high-frequency experimental noise, we impose a criterion such that if \(|\tilde{R}_k| < \gamma\), \(\tilde{R}_k\) is set to 0. The value of \(\gamma\) will be optimized by minimizing the cost function through the loop. 

Step 3: Multiply \(\tilde{R}_k\) by \(2\pi ki/T\) to get \(\hat{R}_k\).

Step 4: Evaluate the inverse DFT of \(\hat{R}\)

\[ \frac{dR}{dt} = \sum_{k=-\frac{N}{2}}^{\frac{N}{2}-1} \hat{R}_k e^{\frac{2\pi i nk}{N}} \]

Step 5: Solve the least-square problem and evaluate the objective function, \(J(C)\).

Step 6: Change \(\gamma\) and return back to step 2 until the value of the objective function stops decreasing.

The thickness \(h\) and the unstressed radius \(R_0\) are directly measured. From the optimization process, we computed the Young’s modulus \(E\) and the viscosity coefficients \(\phi\) and \(\phi_{NL}\) as well as the unsteady radius \(R_0\) again. We will show that the measured and optimized values of \(R_0\) are equivalent.

We note that we have performed the optimization process for a given imposed physiological frequency given by the Jarvik device, but we know that the model parameters depend on the frequency. Therefore, we are supposing that the model (both linear or nonlinear) is valid for all the frequencies, and this is a strong hypothesis when we use only one imposed frequency. To confirm that hypothesis, we need to design an optimization process for large band frequencies and show that the optimal parameters are independent of the input frequency. Finally, once the optimal coefficients are found, we can introduce them into the numerical model to study the wave propagation in the network.

2.3 Simulation of Pulse Waves With the 1D Model. For blood flow in arteries, denoting the circular cross-sectional area by \(A\), the flow rate by \(Q\), and the internal pressure by \(P\), the conservation of mass and balance of momentum follows two partial differential equations (PDEs):

\[ \partial A / \partial t + \partial Q / \partial x = 0 \]

\[ \partial Q / \partial t + \partial (Q^2 / A) / \partial x + A \partial P / \partial x = -C_f Q / A \]

where \(x\) is the axial distance, and \(t\) is the time. The blood density \(\rho\) is here constant, and \(C_f\) is the skin friction coefficient which depends on the shape of the velocity profile. In general, the profile depends on the Womersley number, \(Re / \sqrt{\nu}\), with \(\nu\) as the angular frequency of the pulse wave and \(\nu\) as the kinematic viscosity of the fluid. In practice, \(C_f\) usually takes an empirical value fitted from the experimental observations. In this study, we assume \(C_f = 0.006\) as fitted for the blood flow in large vessels with a Womersley number of about 10 [16]. To close the system of equations, we need a constitutive equation for the pressure \(P\) (Eq. (5)) and is then written

\[ P = P_{ext} + \beta \left( \sqrt{A} - \sqrt{A_0} \right) + \nu_s \frac{\partial A}{\partial t} + \nu_{NL} \left( \frac{\partial A}{\partial t} \right)^2 \]

with

\[ \beta = \frac{\sqrt{\pi} \phi h}{(1 - \eta^2) A_0}, \quad \nu_s = \frac{\sqrt{\pi} \phi h}{2(1 - \eta^2) \sqrt{A_0}}, \quad \nu_{NL} = \frac{1}{4} \left(1 - \eta^2\right) 1/\sqrt{2} A_0 \]

as the elastic and viscoelastic coefficients. Those are the governing equations for the blood flow in one segment.

In the numerical simulations, we preserved the conservation of mass and static pressure at the confluence points between segments. We neglected the energy loss due to the variation of geometry. We impose a flow rate as input condition at the inlet of the network (ascending aorta). The flow rate is a cyclic half sinusoidal function in time of a period of 0.5 s; the simples one having the right signal characteristic in terms of physiological amplitude and frequency. A more physiological waveform shape does not change significantly the numerical results, which are primarily affected by the confluence reflections and terminal resistances. At each outlet, we imposed an identical small reflection coefficient \(R_c = 0.3\).

We solved the governing equations numerically using a finite volume approach by a monotonic upstream scheme for conservation laws (MUSCL). The code has been favorably validated with analytic results and experimental data, see Refs. [17,18].

3 Results and Discussion

3.1 Parameters of the Arterial Wall. Before the complete presentation of the nonlinear Kelvin–Voigt model optimization
results, we discuss the differences in predictions when using a classical linear model and the relative importance of the nonlinear term in $\varepsilon^2$.

Figure 2 presents in the ascending aorta the prediction of the linear model ($E_{NL}$ and $\phi_{NL}$ set to zero), and the nonlinear Kelvin–Voigt model proposed is

$$\left(1 - \eta^2\right)\frac{R}{h}p = E\varepsilon + \phi_0\dot{\varepsilon} + \phi_{NL}\varepsilon^2$$  \hspace{1cm} (9)

The linear model fits poorly the curvature observed in the experimental data (Fig. 2 (left)) and is equivalent to the optimization analysis of Valdez-Jasso et al. \[11\], which adopts a stress relaxation constant as an extra parameter into a linear Kelvin–Voigt model. On the contrary, the nonlinear prediction (Fig. 2 (right)) properly follows the experimental data. We note that linear and nonlinear optimal parameters for ($E$, $\phi_0$) computed independently are very similar: linear ($1.475$ MPa and $26.156$ kPa s) and nonlinear ($1.539$ MPa and $25.451$ kPa s).

From the experimental data of Fig. 2, we can evaluate the order of magnitude of $\varepsilon$ which is around $1.5/10$; therefore, the nonlinear term scales as $\varepsilon^2 \sim 2 \times 10^{-2}$. As the ratio $E_{NL}/E$ is around $10^{-2}$ as shown by the numerical results gathered from the optimization process with the nonlinear parameter $E_{NL}$, the linear term scales as $E\varepsilon$ and the nonlinear one as $10^{-2}E\varepsilon$. The numerical predictions using the nonlinear term $E_{NL}$ confirm that this nonlinear term as small influence and can be neglected as already advanced in Ref. \[8\].

Over the subsequent optimizations we used the nonlinear Kelvin–Voigt model (Eq. (1)). As stated in the Introduction, there are other models for the viscoelasticity (see, e.g., Refs. \[4,8,19,20\]). Fung’s quasi-linear model is more generalized than the spring–dashpot models, but its incorporation in 1D fluid models is complex, thus it is only applicable to limited formulations (e.g., linearized 1D model \[4,8\]).

The results presented in Fig. 3 from the upper left side to the bottom right side (proximal descending aorta, medial descending aorta, distal descending aorta, brachiocephalic trunk, carotid artery, and femoral artery) show that this model captures the wall viscosity and the nonlinearity of the pressure–radius loop. As stated above, Valdez-Jasso et al. \[11\] already tested the Kelvin model simulating the two stress relaxation constants and their results are close to the linear Kelvin–Voigt model. Their sensitivity analysis shows that the model prediction depends least on this constant among all the parameters, thus even though the Kelvin–Voigt does not include this constant, the validity is hardly influenced. Moreover, in contrast to nonlinear optimization methods that estimate the model parameters in Ref. \[11\], we use the linear regression method which is fast and the global optimization is readily guaranteed.

Figure 3 shows the hysteresis in the pressure–radius loop for six arteries (the seventh, the ascending aorta is in Fig. 2). The agreement between the experimental measurements and the model predictions shows that the nonlinear Kelvin–Voigt model captures the wall viscosity everywhere. We remark that among the seven arteries, the brachiocephalic trunk has the largest nonlinearity (Fig. 3 (center and left)).

At the aorta, the nonlinearity decreases from the proximal part to the distal end. Finally, at the peripheral arteries, represented by carotid artery and femoral artery, the nonlinearity is negligible.

We present the unstressed ratio $R_0$, with error bars in Fig. 4, and the mean values are [ascending aorta, proximal descending aorta, medial descending aorta, distal descending aorta, brachiocephalic trunk, carotid artery, femoral artery] = $[0.9489, 0.8809, 0.8554, 0.8286, 0.9002, 0.4069, 0.2826]$. These values compare extremely well the experimentally measured ones $[0.9360, 0.8600, 0.8500, 0.8250, 0.8900, 0.4060, 0.2810]$ (crosses in figure). The experimental measurements of neutral vessel radius are only possible in vitro experiments but impossible in an in vivo analysis, this is the reason we chose to estimate the values of the radius $R_0$ in numerical simulations. Since the nonlinear Kelvin–Voigt model predicts the actual values (within the error bars), which suggests that this approach could be used in an in vivo situation.

Figure 5 (left) shows the Young’s modulus for the seven arteries, and these results have to be compared to those of the linear viscoelastic modulus $E$ in Fig. 5 (right). Both predicted values follow the same behavior. By examining the parameter values among the different arteries, we can see that smaller arteries tend to be stiffer, as pointed out by previous studies \[11,20\]. We note that running the optimal process for the linear model we found similar values of $E$ and $\phi_0$, this implies that these parameters are unaffected by the nonlinear coefficient and suggests that at the first-order they have a physical meaning.

We analyzed the relation between the Young’s modulus and the viscoelastic coefficient by defining a characteristic time $\phi_0/E$. Figure 6 presents the values for the seven arteries: an important observation is that these values seem to be constant.

We want to stress in this study the importance that the ratio between $\phi_0$ and $E$ is constant and the impact this has on high frequencies components of the pulse waves. From the linear Kelvin–Voigt equation (9), with $\phi_{NL} = 0$, the magnitude of the complex modulus is $|G| = E \sqrt{1 + (\tau_r/\tau_f)^2}$, where $\tau_r = \phi_0/E$ is the viscoelastic relaxation time, and $\tau_f = 1/\omega$ is the typical forcing time. The linear model also gives the phase shift as $\delta = \arctan(\tau_r/\tau_f)$. Therefore, for an imposed pressure perturbation on a viscoelastic arterial wall, the wall will come back to its equilibrium state but with a phase lag characterized by the viscoelastic relaxation time. Figure 6 shows that the viscoelastic relaxation time seems to be a biological constant. It is then evident that for high values of $\omega$, the pressure perturbations vanish as long as $\arctan(\tau_r/\tau_f) \to \pi/2$. The pressure perturbation and the wall response will be in phase opposition. This indicates that higher frequency of the waves will lead to stronger damping effect of the
wall viscosity. Since the wavefronts are more steepened toward the peripheral part of the arterial tree due to the advection effect of blood flow, the damping effect is more significant in this part. Damping effect maybe a protective factor of the microcirculatory system.

In a stiffer vascular network, pulsatile energy at high frequency tends to be damped in microcirculation, especially in the brain and kidney [21]. The arterial wall is mainly composed of elastin and muscular fibers and this composition varies throughout the whole network, from the aorta to the peripheral arteries. The elastin is more related with the elasticity modulus and the muscular fibers to the viscoelasticity. The smaller arteries usually have more muscular fibers than large arteries, and this may also be explained by the need of a stronger damping factor of pulsations right before the microcirculations.

Finally, the mean values of the ratio }_{NL} \phi / \phi \text{ are for ascending aorta, proximal descending aorta, medial descending aorta, distal descending aorta, brachiocephalic trunk, carotid artery, and femoral artery equal to } \left[-0.915, -0.999, -0.888, -0.975, -1.380, 0.524, -0.395\right]. This result allows to estimate the order of magnitude of the terms in } \dot{\varepsilon} \text{, this is } \phi_0 \dot{\varepsilon} \text{ and } \phi_{NL} \dot{\varepsilon}^2 \text{. Writing } \phi_0 \dot{\varepsilon} + \phi_{NL} \dot{\varepsilon}^2 \text{ from Eq. (9) as } \phi_0 \dot{\varepsilon} \left(1 + \left(\phi_{NL} / \phi_0\right) \dot{\varepsilon}\right), \text{ we observe that both } \phi_{NL} / \phi_0 \text{ and } \dot{\varepsilon} \text{ are of the order 1 as long as } \dot{\varepsilon} \text{ is evaluated as

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Fig. 3 Experimental data and the fitted nonlinear Kelvin–Voigt model. Parameter values are in Table 1.

Fig. 4 Optimal unstressed radius } R_0 \text{, predicted and measured for the seven arteries (ascending aorta, proximal descending aorta, medial descending aorta, distal descending aorta, brachiocephalic trunk, carotid artery, and femoral artery)
\[
\frac{(1/10)(2\pi/T)}{\varepsilon}, \quad \text{where } 1/10 \text{ is the amplitude of } \varepsilon, \text{ and } T \text{ is the imposed signal period.}
\]

### 3.2 Pulse Waves

We propose a 1D numerical model to put forward the differences between an elastic and a viscoelastic wall model. We set the nonlinear viscoelastic coefficient \( \phi_{NL} \) to zero for simplicity. Preliminary simulations show that the behavior is similar and not particular shape or pattern was found. The nonlinear term could play a role in a transient state in large networks.

We use the mean values coming from the optimization process. Table 1 shows the parameters of the simulated arterial tree where the length \( L \) of each artery is estimated from the data in literature [15].

To model the terminal branches of the aorta, we added three virtual arteries (VAs) at the ends of proximal descending, medial descending, and distal descending aorta, respectively (see Fig. 1). We determined the radius of the virtual arteries by Murray’s law and we calculated their elasticity using a well-matched condition which is essentially no reflections at the bifurcations.

At the inlet of the network (ascending aorta), the flow rate is a cyclic half sinusoidal function in time with a period of 0.5 s, and the peak value is \( Q_{\text{max}} = 55 \text{cm}^3/\text{s} \). As long as the pressure waves travel in the network, high-frequency components appear in the signal due to reflexions and the branching points and because the vessel segments are short, geometrically reducing the wavelength of the pulse waves.

Figure 7 presents the simulated results of flow rate at two different representative locations: medial descending aorta (left) and carotid artery (right) for peripheral arteries. The elastic wall model shows high-frequency components, especially on the carotid artery. With the viscoelastic wall model, we observe on the contrary that the high-frequency components of the waveform are damped.

Previous numerical studies [3,4,6–8] have shown the significant damping effect of wall viscosity on the pulse waves but limited by
the lack of exactitude of the values of the model parameters, especially for the viscoelasticity of the arterial network. In our numerical simulations, we use estimates of the viscoelasticity by evaluating the pressure–diameter relationship from a dataset of direct measurements on arterial network of sheep.

One of the major drawbacks of numerical simulation on extended networks is the impossibility of computing the viscoelastic coefficients directly from the experimental data. On the contrary, the Young’s modulus is well known and a large literature exists. If we work with the hypothesis that the ratio between the Young’s modulus is almost constant, we will be able to build networks using accessible information.

4 Conclusion

We estimated the viscoelasticity of the arterial network of a sheep by evaluating the pressure–diameter relationship with a dataset of direct measurements. Good agreements between the proposed nonlinear Kelvin–Voigt model and measurements were achieved through a linear regression method. The obtained parameter values were used in a 1D blood flow model to simulate the pulse waves in the arterial network. We have shown the damping effect of the wall viscosity on the high-frequency waves, especially at the peripheral arteries. We explained it by the nearly constant value of the viscoelastic relaxation time, defined by the ratio between the viscosity coefficient and the Young’s modulus. The optimal values of the ratio $\phi_{NL}/\phi$ seem to be constant in five of the seven arteries, we plan for a future work to study the impact of the nonlinear coefficient $\phi_{NL}$ in large networks.

References


